

## Math 53, Fall 2025, Section 104, Quiz 3

Name: \_\_\_\_\_

Student ID: \_\_\_\_\_

Time limit: 20 minutes.

- *Please keep your work only on the two printed pages.*
- *An answer without any work shown will get no credit.*

If a problem asks for a specific answer (rather than an explanation), box your result. You do not need to simplify expressions such as  $2(x-1) + x$ , but you should evaluate trigonometric functions of simple angles such as multiples of  $\frac{\pi}{4}$  and  $\frac{\pi}{6}$ .

1. (5 points each, **part (b) is extra credit**) For each region  $R$ , write the area integral  $\iint_R dA$  as two equivalent double integrals: one in terms of  $dx dy$  and one in terms of  $dy dx$ . You *do not* need to evaluate the integrals. Answers with variables out of scope (as in  $\int_x^1 \int_1^0 dx dy$ ) will receive little or no credit. (*Hint: drawing the regions will help!*)
  - (a)  $R$  is the triangle with vertices  $(6,7)$ ,  $(7,7)$ , and  $(7,8)$ .
  - (b) *Your answer to this one cannot be a sum of integrals.*  $R$  is the triangle with vertices  $(0,0)$ ,  $(2,2)$ ,  $(-2,2)$ .

2. (5 points each) Evaluate each of the following integrals.

(a)  $\int_3^6 \int_5^7 \left(\frac{1}{x} + xy\right) dy dx.$

(b)  $\int_{-1}^0 \int_y^{y^2} y dx dy.$

3. (10 points) Use Lagrange multipliers to find the distance between the point  $(1, 2, -2)$  and the nearest point on the surface  $x^2 + y^2 + z^2 = 16$ , as well as the location of that point (or points). **Extra credit: find a solution that doesn't use derivatives at all.**