

## Topics in Cluster algebras, Fall 2016

**Professor:** Lauren Williams

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**Time and place:** MW 11:40am-12:55pm, 520 Mathematics building

**Website for course:** <https://math.berkeley.edu/~williams/Columbia-CA.html>

**Office Hours:** Room 512, Mathematics building, by appointment.

### **Course description and prerequisites:**

This course will survey one of the most exciting recent developments in algebraic combinatorics, namely Fomin and Zelevinsky's theory of cluster algebras. Cluster algebras are a class of combinatorially defined commutative rings that provide a unifying structure for phenomena in a variety of algebraic and geometric contexts. Introduced in 2000, cluster algebras have already been shown to be related to a host of other fields of math, such as quiver representations, Teichmüller theory, Poisson geometry, total positivity, and integrable systems.

I will not assume prior knowledge of cluster algebras, but I will assume that the students have a solid background in graduate-level algebra. Familiarity with root systems will be helpful for a few of the lectures.

### **Course goals:**

The goal is for students to gain a concrete understanding of cluster algebras and some of the basic techniques for working with them.

### **References:**

S. Fomin, L. Williams, and A. Zelevinsky, Introduction to cluster algebras, Chapters 1-3, <http://front.math.ucdavis.edu/1608.05735>.

L. Williams, Cluster algebras: an introduction, Bulletin of the AMS, 2014.

S. Fomin and A. Zelevinsky, Cluster algebras I, II, IV.

**Course requirements and grading:** Students will be required to write a final paper. The final grade will be based on this paper.

### Weekly breakdown of topics:

<u>Date</u>	<u>Topics</u>
Week 1	Total positivity
Week 2	Mutation
Week 3	Cluster algebras of geometric type
Week 4	The Laurent phenomenon
Week 5	Rank 2 cluster algebras
Week 6	Cluster algebras from surfaces and Teichmuller theory
Week 7	Finite type classification of cluster algebras; folding
Week 8	Cluster structures in coordinate rings
Week 9	Cluster structures on Grassmannians
Week 10	Total positivity for Grassmannians
Week 11	Quantum cluster algebras
Week 12	TBD
Week 12	TBD

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If you have been certified by Disability Services (DS) to receive accommodations, please either bring your accommodation letter from DS to your professors office hours to confirm your accommodation needs, or ask your liaison in GSAS to consult with your professor. If you believe that you may have a disability that

requires accommodation, please contact Disability Services at 212-854-2388 or [disability@columbia.edu](mailto:disability@columbia.edu).

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