

1. Find the number of elements in $A_1 \cup A_2 \cup A_3$ if there are 100 elements in each set and 50 ~~are~~ elements in each of $A_1 \cap A_2$, $A_2 \cap A_3$ and $A_1 \cap A_3$, and none in all three sets.
2. Find the number of integers from 1 to 100 that are either odd or a square.
3. Find the number of ~~integer~~ solutions to $x_1 + x_2 + x_3 = 15$ where ~~all~~ $x_1, x_2, x_3 \leq 6$ are integers.
4. An integer is squarefree if it is not divisible by any perfect square greater than 1. Find the number of squarefree positive integers less than 100.
5. List all the derangements of $\{1, 2, 3, 4\}$.
6. Prove the principle of inclusion-exclusion using mathematical induction.