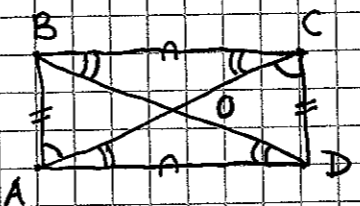


1.5.



$AB \parallel CD$
 $BC \parallel AD$ by I.27

$\triangle ABC \cong \triangle CDA$ by ASA

$AB \cong CD$ $\Rightarrow \triangle ABC \cong \triangle DCB$ by SSA

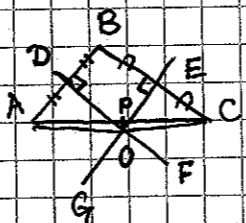
$BC \cong AD$

$\Rightarrow AC \cong BD$

$\triangle OBC, \triangle OCD, \triangle ODA, \triangle OAB$ isosceles by I.6

Hence $BO \cong OC \cong OD \cong OA$

1.9.



DF perpendicular bisector to AB
 GE perpendicular bisector to BC

We claim that they meet at some point O. Indeed, if they are parallel then by I.27 AB and BC are also parallel. Contradiction.

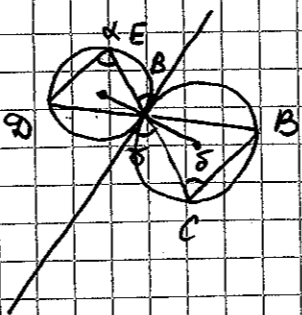
$OA \cong OB$ since $\triangle OAD \cong \triangle ODB$ SAS

Similarly $OB \cong OC$. So $OA \cong OC$

Let $OP \perp AC$. Then $\triangle OAP \cong \triangle OPC$ RASS So $AP \cong PC$

and OP is a perpendicular bisector to AC.

1.13



By III.12
 Draw a line through the centers of two circles. The line tangent to both circles is perpendicular to this line by III.16.

Then we have $\alpha \cong \beta$ by III.32

$\beta \cong \gamma$ (vertical), $\gamma \cong \delta$ by III.32 again.

Hence ED is parallel to BC by I.28

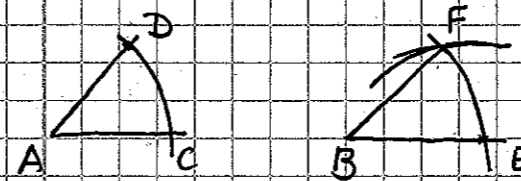
2.5. 1) Point C, $\odot c_A \cap AC$ Get D

2) $\odot c_B \cap AC$ Get E

3) $\odot c_E \cap CD$ Get F

4) BF

$\angle DAC \cong \angle FBE$ because $\triangle ADC \cong \triangle BFE$ (SSS)



2.6. 1) Choose A on a circle. $\odot c_A$, get B and C.

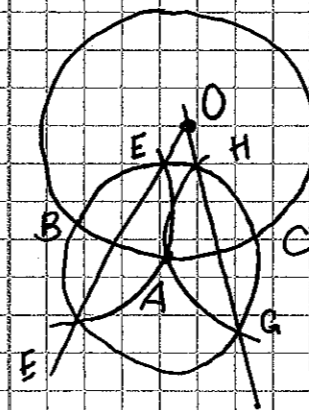
2) $\odot c_B \cap AB$ Get E, F

3) $\odot c_C \cap AB$ Get G, H

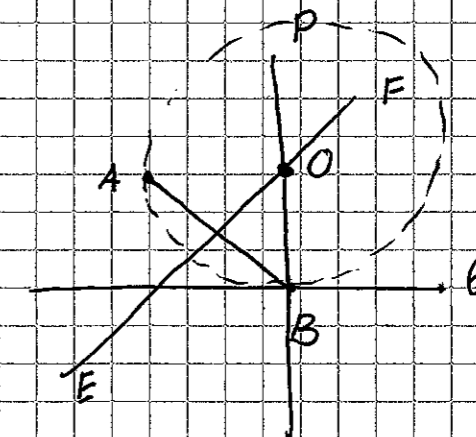
4) Line EF

5) Line GH

EF and GH meet at O (the center of the circle)
(equal distances $OB \cong OA \cong OC$)



2.12.

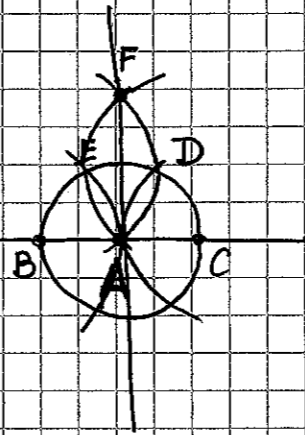


1) EF perpendicular bisector to AB (3 steps)

2) $PB \perp l$ (4 steps)

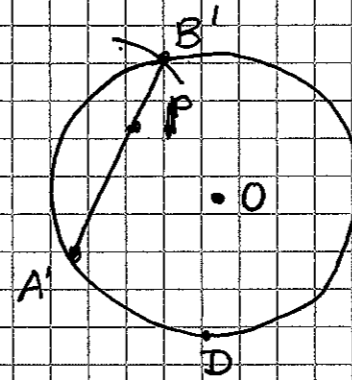
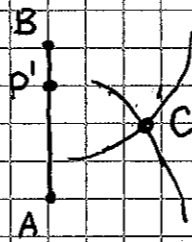
3) $\odot c_O \cap OB$

2.17.



- 1). $\odot c A$ points B & C
- 2). $\odot c B$ point E
- 3). $\odot c C$ point D
- 4). $\odot c E$
- 5). $\odot c D$ point F
- 6). line $FA \perp BC$

2.22



- 1). D a point on the circle
- 2). $\odot c B \cap OD$
- 3). $\odot c A \cap OD$ get C
- 4). $\odot c C \cap OP$ get P'
- 5). $\odot c P \cap B'P'$ get B'
- 6). $B'P$

$BA \cong B'A'$ since

$$\triangle CAB \cong \triangle OA'B'$$

$$\triangle P'CB \cong \triangle P'OB'$$