$\begin{array}{c} \text{PROBLEM SET } \# \ 9 \\ \text{MATH 249} \end{array}$

Due October 7.

- **1**. Find explicit formulae for the quasi polynomials $\bar{p}_3(n)$ and $\bar{p}_4(n)$.
- 2. Bus tickets in Moscow always have six digit numbers. A ticket is lucky if the sum of the first 3 digits equals the sum of the last 3 digits. Find the number of lucky tickets.
- 3. Let C be a pointed convex polyhedral cone, Γ and Γ' be triangulations of C whose extreme rays are the same as the extreme rays of C. Let γ_k be the number of faces of Γ of degree k. Is it always true that $\gamma_k = \gamma_k'$?

Date: October 31, 2006.