

Problem Set for Rocky's 1st Lecture

Fibonacci

Problem 1. Use the closed form of the Fibonacci numbers to compute the first 5 negative Fibonacci numbers. How are they related to the first 5 positive Fibonacci numbers?

$$F_n = \frac{\left(\frac{1+\sqrt{5}}{2}\right)^n - \left(\frac{1-\sqrt{5}}{2}\right)^n}{\sqrt{5}}$$

Problem 2. In class we saw we could sum $1+2+3+4+\dots+n$ as $n(n+1)/2$

Check that we can sum $1^2 + 2^2 + 3^2 + \dots + n^2$ as $n(n+1)(2n+1)/6$

I.e. Check the first 4 or so and see that it works

Problem 3. Show that $F_1 + F_2 + F_3 + \dots + F_n = F_{n+2} - 1$

Hint: Remember that $F_{n+1} = F_n + F_{n-1}$