# Quiz 1 Solutions <br> MATH 1A Fall 2015 

## 10 September 2015

Exercise 1.1. Prove

$$
\lim _{x \rightarrow 6} \frac{x}{2}=3
$$

Proof. Let $\varepsilon>0$. Set $\delta=2 \varepsilon$.
Suppose $0<|x-6|<\delta$. Then

$$
\left|\frac{x}{2}-3\right|=\frac{1}{2}|x-6|<\frac{1}{2} \delta=\frac{1}{2} \cdot 2 \varepsilon=\varepsilon
$$

Thus for every $\varepsilon>0$ there is a $\delta>0$, namely $\delta=2 \varepsilon$, such that if $0<|x-6|<\varepsilon$ then $\left|\frac{x}{2}-3\right|<\varepsilon$. This proves $\lim _{x \rightarrow 6} \frac{x}{2}=3$.

Exercise 1.2. Write down the truth table for the statement "(not P) and Q".
Solution.

|  |  | $P$ |  |
| :---: | :---: | :---: | :---: |
|  |  | T | F |
|  | T | F | T |
| Q |  |  |  |
|  | F | F | F |

