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Let V and W be vector spaces over a field F . Suppose that $f : V \rightarrow W$ satisfies $f(v + w) = f(v) + f(w)$ for $v, w \in V$. Assume that $f(v) = 0$ if and only if $v = 0$.

Show that f is injective (i.e., f is 1-1).