## Math 10A Homework #9; Due Tuesday, 7/24/2018 Instructor: Roy Zhao

- 1. Verify that  $a_n = 2 \cdot 3^n + 1$  is a solution to the recurrence relation  $a_n = 4a_{n-1} 3a_{n-2}$ .
- 2. Verify that  $a_n = 2^n 1$  is a solution to the recurrence relation  $a_n = 2a_{n-1} + 1$  with  $a_0 = 0$ .
- 3. Verify that both  $a_n = 2^n 3^n$  and  $a_n = 2^n$  are solutions to the recurrence relation  $a_n = 5a_{n-1} 6a_{n-2}$ .
- 4. Find A, B such that  $a_n = An + B$  is a solution to the recurrence relation  $2a_n = a_{n-1} + 2a_{n-2} + n$ .
- 5. For each of the following recurrence relation, find their order and determine whether they are homogeneous, linear, and/or constant coefficient.

(a) 
$$a_n = a_{n-1} - a_{n-2}^2$$

(b) 
$$a_n = n a_{n-3}$$

- (c)  $a_n = a_{n-2}^3 a_{n-4} + 3$
- (d)  $a_n = 2a_{n-1} a_{n-2}$

(e) 
$$a_n = a_{n-1} + 1$$