MATH 54 SUMMER 2017, QUIZ 23

Find the projection of $\sin(x)$ on the subspace $\operatorname{span}\{1,x\}$ in the inner product space $C([0,\pi])$ with the inner product given below.

$$\langle f, g \rangle = \int_0^{\pi} f(x)g(x) dx$$

Warning: with the inner product above, $\{1, x\}$ is not an orthogonal set!

[Hint:
$$\int_0^{\pi} \sin(x) dx = 2$$
 and $\int_0^{\pi} x \sin(x) dx = \pi$.]

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