

1. Let A be a commutative ring and let p be a prime which vanishes in A . Suppose that $f \in A[x]$ satisfies $f'(x) = 0$, and that $a \in A$ with $f(a) = 0$. Show that $(x - a)^p$ divides $f(x)$.