Match the differential equation to the corresponding vector field,

$$\frac{dy}{dx} = y \qquad \frac{dy}{dx} + \frac{1}{2}y = x \qquad \frac{dy}{dx} = x(y+1) \qquad \frac{dy}{dx} = \frac{x}{y}$$



Solve the following first order differential equations using any method of your choosing,

(1) 
$$y' = \frac{y(x+2)}{x}$$

(2) 
$$\frac{dy}{dx} = x^2y + x^5, \quad y(0) = 1$$

(3) 
$$y' = (x^2 + 1)y$$

(4) 
$$y' - 2y = x^2 e^{2x}$$
,  $y(0) = 2$ 

(5) 
$$x\frac{dy}{dx} = y + x^2 \sin x, \quad y(\pi) = 0$$

(6)  $x^2y' + 2xy = 1$ 

Solve the following second order differential equations using any method of your choosing,

(1) 
$$y'' - 3y' + 2y = 0$$

(2) 
$$y'' + 4y' + 4y = e^x$$
,  $y(0) = 1$ ,  $y'(0) = -1$ .

(3) 
$$y'' + 9y = \sin x + \cos x$$

(4) 
$$y'' - y' = e^x + x$$
,  $y(0) = 1$ ,  $y'(0) = 1$ 

(5) y'' + 4y = 8

(6) 
$$y'' - 2y' + 4y = 8x - 12\sin(2x), \quad y(0) = -2, \quad y'(0) = 8$$