

p. 114 # 3

$$\begin{aligned}\cos(z) &= \sqrt{2} \\ \frac{1}{2}(e^{iz} + e^{-iz}) &= \sqrt{2} \\ e^{iz} + e^{-iz} &= 2\sqrt{2} \\ e^{2iz} + 1 &= 2\sqrt{2}e^{iz} \\ e^{2iz} - 2\sqrt{2}e^{iz} + 1 &= 0 \\ (e^{iz} - \sqrt{2})^2 - 1 &= 0 \\ e^{iz} - \sqrt{2} &= \pm 1 \\ e^{iz} &= \sqrt{2} \pm 1 \\ iz = \log(\sqrt{2} \pm 1) &= \ln(\sqrt{2} \pm 1) + 2\pi in \\ z &= 2\pi n - i \ln(\sqrt{2} \pm 1)\end{aligned}$$