Math 54: Quiz #2

February 2 GSI: M. Lindsey

Please give neat and organized answers. Whenever applicable (especially for computational questions), make it clear what strategy you are using.

Problem 1

Let

$$A = \left[\begin{array}{rrr} 1 & 2 & 1 \\ -3 & -1 & 2 \\ 0 & 5 & 3 \end{array} \right].$$

Do the columns of A span \mathbb{R}^3 ?

Problem 2

Let

$$\mathbf{v}_1 = \begin{bmatrix} 1 \\ 2 \\ 1 \end{bmatrix}, \ \mathbf{v}_2 = \begin{bmatrix} 2 \\ 2 \\ 2 \end{bmatrix}, \ \mathbf{v}_3 = \begin{bmatrix} -4 \\ -2 \\ h \end{bmatrix}.$$

(a) For what values of h is \mathbf{v}_3 in $\mathrm{Span}\{\mathbf{v}_1,\mathbf{v}_2\}?$

(b) For what values of h is $\{\mathbf{v}_1,\mathbf{v}_2,\mathbf{v}_3\}$ linearly dependent?