## Math 1B: Calculus Discussion Section 2

## WORKSHEET 6

Prove (make an argument!) that following series are absolutely convergent, conditionally convergent, or divergent.
(a)

$$
\sum_{n=1}^{\infty}\left(1+\frac{1}{n^{3}}\right)^{\pi / n+n^{2}}
$$

(b)

$$
\sum_{n=0}^{\infty}\left(\frac{2-3 \sin (n)}{6}\right)^{n}
$$

(c)

$$
\sum_{n=0}^{\infty}\left(\frac{n}{n+3}\right)^{n^{2}}
$$

(d)

$$
\sum_{n=0}^{\infty}(\sqrt[n]{2}-1)
$$

(e)

$$
\sum_{n=1}^{\infty}(-1)^{n}\left(\sin \left(\frac{1}{n}\right)\right)^{1 / 3}
$$

(f)

$$
\sum_{n=0}^{\infty}\left(\frac{1}{1+3 \cdot(-1)^{n}}\right)^{n}
$$

Classifying Tests for Convergence and Divergence

| Test name | Example of series to test | Conditions on series to be <br> tested | Conclusions you can draw <br> from this test |
| :--- | :--- | :--- | :--- |
| p-Series |  |  |  |
| Geometric Series |  |  |  |
| Comparison |  |  |  |
| Ratio |  |  |  |
| Root |  |  |  |
| Alternating Series |  |  |  |

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