

Name: \_\_\_\_\_

Section: \_\_\_\_\_

## Math 54 Lec 006 Quiz 5

Friday, July 06, 2018

Justify your assertions; include detailed explanation, and show your work. Closed book exam, no sheet of notes and no calculator. This quiz is worth 9 points total.

1. (3 points) Let

$$H = \left\{ \begin{pmatrix} a \\ b \\ c \\ d \end{pmatrix} : a - 2b + c = 0, 2b + 3c = 0, a + b + 4c = 0 \right\}$$

be a subspace of  $\mathbb{R}^4$ . Find a basis for  $H$  and state the dimension of  $H$ .

2. (3 points) Let  $B = \{7 + 5x, -3 - x\}$  and  $C = \{1 - 5x, -2 + 2x\}$  be two basis for  $P_1[x]$ , find the change-of-coordinates matrix from  $B$  to  $C$ .

3. (3 points) True or False: If  $T$  is a linear transformation from  $V$  to  $\mathbb{R}^4$ , and if  $\ker(T) = \{0\}$ , then  $\dim(V) \leq 4$ .