Math 54 Handout 19

August 3, 2018

Question 1.

Find the eigenvalues λ and eigenfunctions of the following:

1.
$$\begin{cases} y'' + \lambda y = 0; \ 0 \le t \le 2\pi \\ y(0) = y(2\pi); \ y'(0) = y'(2\pi) \end{cases}$$

2.
$$\begin{cases} y'' + \lambda y = 0; \ 0 \le t \le \pi/2 \\ y'(0) = 0; \ y'(\pi/2) = 0 \end{cases}$$

Question 2.

Compute the Fourier series for

$$f(x) = \begin{cases} -1, & -\pi \le x \le 0\\ 1, & 0 \le x \le \pi \end{cases}$$