Math 53 - Multivariable Calculus

Quiz # 1

September 1st, 2011

Exercise 1. Describe the motion of a particle with position (x(t), y(t)), where $x(t) = 2\sin(t)$, $y(t) = 4 + \cos(t)$ and $0 \le t \le \pi$.

Exercise 2. Set up an integral, but do not evaluate, that represents the length of the curve given by $x(t) = t - t^2$, $y(t) = \frac{4}{3}t^{3/2}$ and $1 \le t \le 2$.

Exercise 3. Identify the following curve,

$$r = 2\sin(\theta) + 2\cos(\theta), \qquad 0 \le \theta < 2\pi,$$

by finding a Cartesian equation of the curve. (Hint: Start by multiplying both sides by r, then convert to Cartesian coordinates and complete the square.)