

Graphing Quadratics.

Idea: Complete the square to turn quadratic polynomial $g(x) = 2x^2 - 4x + 3$ into a vertex form $g(x) = A(x-h)^2 + k$.

Then, realize that the graph of $g(x)$ is related to graph of $f(x) = x^2$ by

- Vertical scaling by A
- Horizontal shift by h
- Vertical shift by k

$$\begin{aligned} g(x) &= 2x^2 - 4x + 3 \\ &= 2(x^2 - 2x) + 3 \\ &= 2(x^2 - 2x + 1 - 1) + 3 \\ &= 2(x^2 - 2x + 1) - 2 + 3 \\ &= 2(x-1)^2 + 1 \\ &= A(x-h)^2 + k \end{aligned}$$

where $A=2$
 $h=1$
 $k=1$

