Name:
Maximizing Area. (8 Pts) Find the maximal area of a rectangle which

- Has sides parallel to the $x$ and $y$ axis
- Has one corner at the origin
- Has opposite corner contained in the shaded region drawn below.


Polar Coordinates. (4 Pts) Write an integral computes the area of the shaded region using polar coordinates.


Double Integrals. (8 Pts) Write double integrals which compute the areas of each of the shaded regions:



Bonus Problem. Worth no points! Can you find a set of numbers $a_{i j}$ where $i, j \in \mathbb{N}$, so that

$$
\sum_{i=1}^{\infty} \sum_{j=1}^{\infty} a_{i j}=1
$$

but

$$
\sum_{j=1}^{\infty} \sum_{i=1}^{\infty} a_{i j}=0
$$

Use these functions to describe a function $f(x, y)$ so that $\iint f d x d y \neq \iint f d y d x$. (This will be in an improper integral.)

