

MATH 1B WEEK 8, TUESDAY

Do the following series converge?

Exercise 1. $\sum_{n=0}^{\infty} \frac{(n!)^2}{(2n)!}$

Exercise 2. $\sum_{n=1}^{\infty} \frac{2^n}{n^{1,000,000}}$

★ **Exercise 3.** $\sum_{n=1}^{\infty} \frac{n^n}{n!}$ (*Hint:* Use the ratio test, and the fact that $\lim_{n \rightarrow \infty} \left(1 + \frac{1}{n}\right)^n = e$.)

For which values of x do the following series converge?

Exercise 4. $\sum_{n=0}^{\infty} \frac{x^n}{4^n}$

Exercise 5. $\sum_{n=0}^{\infty} (n^3 + 1)x^n$

★ **Exercise 6.** $\sum_{n=1}^{\infty} \frac{n^2 + 1}{n^x}$ (This is *not* a power series!)