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GSI: Jeremy Meza
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1. Find a closed form for the generating functions of the following sequences (2 points each).
(a) $a_{n}=3^{n}+1$
(b) $a_{n}= \begin{cases}2 & : n \text { even } \\ -2 & : n \text { odd }\end{cases}$
(c) $a_{n}= \begin{cases}1 & : 5 \mid n \\ 0 & : \text { else }\end{cases}$
2. (a) Find a recurrence relation for the number of bit strings of length $n$ that contain a pair of consecutive 0 s (2 points).
(b) How many bit strings of length 7 contain a pair of consecutive 0s? (2 points).
