1. Find a closed form for the generating functions of the following sequences (2 points each).

(a)
$$a_n = 3^n + 1$$

(b)
$$a_n = \begin{cases} 2 & : n \text{ even} \\ -2 & : n \text{ odd} \end{cases}$$

(c)
$$a_n = \begin{cases} 1 & :5 \mid n \\ 0 & : \text{else} \end{cases}$$

2. (a) Find a recurrence relation for the number of bit strings of length n that contain a pair of consecutive 0s (2 points).

(b) How many bit strings of length 7 contain a pair of consecutive 0s? (2 points).