

Math 55 Quiz 2  
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1. True or False? No justification needed.

(a)  $\{x \in \mathbb{R} \mid x^2 + 1 = 0\} \subseteq \mathbb{Z}$ .

(b) The function  $f: \mathbb{Z} \rightarrow \mathbb{Z}$  given by  $f(x) = x^3$  is one-to-one.

(c) If  $A$  and  $B$  are both countable, then so is  $A \cup B$ .

2. Let  $f: A \rightarrow B$  be a function from sets  $A, B$ . Define what it means for  $f$  to be onto.

3. Let  $f: A \rightarrow B$  be a function. Given a subset  $S \subseteq B$ , define  $f^{-1}(S) = \{x \in A \mid f(x) \in S\}$ .  
Given  $S, T \subseteq B$ , prove that  $f^{-1}(S \cap T) = f^{-1}(S) \cap f^{-1}(T)$ .