

**I.5.2.** Prove that if  $z_1$  and  $z_2$  are complex numbers, then  $|z_1 - z_2| \geq ||z_1| - |z_2||$ . Determine the condition for equality.

**I.7.4.** Prove that the distinct complex numbers  $z_1, z_2, z_3$  are the vertices of an equilateral triangle if and only if

$$z_1^2 + z_2^2 + z_3^2 = z_1z_2 + z_2z_3 + z_3z_1.$$

**I.11.1.** Find all cube roots of  $i$ .

**I.11.4.** Prove that the sum of the  $n$ -th roots of 1 equals 0 ( $n > 1$ ).

**I.14.1.** Establish the formula

$$\rho(z, \infty) = \frac{2}{\sqrt{|z|^2 + 1}}.$$

Here  $\rho(z, \infty)$  is the Euclidean distance between the image of the point  $z$  of the complex plane under the stereographic projection and the North pole of the sphere (representing the infinity  $\infty$ ).