## MATH 53 DISCUSSION SECTION PROBLEMS - 1/26/23

## 1. Areas and lengths in polar coordinates

(1) (textbook 10.4.7) Find the area of the region which is inside the curve $r=4+3 \sin \theta$ and to the right of the $y$-axis.
(2) (textbook 10.4.19) Find the area of the region enclosed by one loop of the curve $r=\sin 4 \theta$.
(3) (textbook 10.4.31) Find the area of the region that lies inside both of the curves $r=\sin 2 \theta$ and $r=\cos 2 \theta$.
(4) (textbook 10.4.45) Find the exact length of the polar curve $r=2 \cos \theta, 0 \leq \theta \leq \pi$.
2. Notes

All problems labeled "textbook" come from Stewart, James, Multivariable Calculus: Math 53 at UC Berkeley, 8th Edition, Cengage Learning, 2016.

Problems marked $\left({ }^{*}\right)$ are challenge problems, with problems marked $\left({ }^{* *}\right)$ especially challenging problems.

