

Chapter 4.1
Wednesday, Week 3

Warmup

1. If I have 7 friends and 30 cookies, and I divide the cookies as evenly as possible among my 7 friends, how many cookies will be left over?
2. True or false: $31103 \times 20775 = 646164821$
3. Today is Wednesday. What day of the week will it be 1440 days from now?
4. Starting at 12:00, I watch 15 movies that last 1 hour and 55 minutes each, with no time in between movies. What will the minute hand of my clock say when I am done?

Modular Arithmetic

What is $(-15) \pmod{7}$? Should it be 6 or -1?

True or False: if $5a \equiv 5b \pmod{12}$ then $a \equiv b \pmod{12}$.

True or False: if $8a \equiv 8b \pmod{12}$ then $a \equiv b \pmod{12}$.

Prove that the product of two odd numbers is odd... the easy way! (What does \mathbb{Z}_2 have to do with odd and even numbers?)

What is $n^2 \pmod{4}$? What is $n^2 \pmod{3}$? (4 and 3 cases, respectively)

Prove that 20101010103 is not a perfect square, using the above.