## 12.2: Vectors

Friday, January 29

## Warmup

1. $\lim _{x \rightarrow 0} \frac{\sin x}{x}=$
2. $\lim _{x \rightarrow 0} \frac{1-\cos x}{x}=$
3. $\lim _{x \rightarrow 0} \frac{1-\cos x}{x^{2}}=$
4. If $y(t)=t^{2}$ and $x(t)=1-\cos t$, what is the slope when $t=0$ ?
5. Alice and Bob find a treasure map, which gives the following instructions:

Go 2 miles north. Go 3 miles east. Go 4 miles west. Go 1 mile south. Go 1 mile west.
(a) How far away from their starting point will they end up?
(b) If they start at the right spot but accidentally follow the instructions in reverse order, how far from the treasure will they end up?

## Vectors!

1. Plot the vector $v=\langle 2,2 \sqrt{3}\rangle$. What angle does it make with the positive x-axis? Note: these numbers are different from the ones presented in class, but the procedure for solving the problems is largely the same.
2. Find a unit vector $u$ that is perpendicular to $v$, and plot $u, u+v$, and $3 u-2 v$ relative to the origin.
3. Find $|v|,|u+v|$, and $|3 u-2 v|$. How is the Pythagorean Theorem relevant?
4. Plot the vectors $w=\langle 1,3\rangle$ and $z=\langle 5,2\rangle$. Plot the vectors $t w+(1-t) z$ for $t=-1,0,1 / 2,3 / 2$. Make observations.

## More Vectors!

1. A box is neither moving nor accelerating (relative to the table it sits on). What is the net force on the box?
2. The three forces $a, b$, and $c$ are acting on the object at $P$, and the net force is zero.


Treating $P=\overrightarrow{O P}, A=\overrightarrow{O A}, B=\overrightarrow{O B}$, and $C=\overrightarrow{O C}$ as vectors starting from the origin (not pictured), express $a, b, c$ in terms of $P, A, B, C$.
3. Given that the net force is zero, express $P$ in terms of $A, B$, and $C$.
4. A boatman wants to cross a canal that is 2 km wide and wants to land on a point 4 km upstream from his starting point. The current in the canal flows at $2 \mathrm{~km} / \mathrm{h}$ and the speed of his boat is $13 \mathrm{~km} / \mathrm{h}$. Note: These numbers have been changed to make the answer nicer.
(a) In what direction should he steer?
(b) How long will the trip take?

