

## Review Problems for Final

1. Graph  $f(x) = \frac{x^2+4x+3}{x-2}$ .
2. Graph  $f(x) = \frac{1}{x} + \sqrt{x}$ .
3. Graph  $f(x) = \sqrt{x^2 - 2}$ .
4. Find a constant  $k$  such that  $\lim_{x \rightarrow 0} \frac{\sin(x)+kx}{x^3}$  exists.
5. Use Newton's Method to find the next two terms for
  - $x^2 - x - 1 = 0, x_0 = 1$
  - $ax - b = 0, x_0 = c$
6. A 10m wire is cut into two pieces, one bent to make a square and the other an equilateral triangle. Maximize/minimize the combined area of the two shapes.
7. Maximize/minimize  $g(x) = \int_{\sin(x)}^{\cos(x)} t dt$
8. Write the Riemann sums for the areas of triangles with the following vertices, and find the corresponding integrals:
  - $(0, 0), (1, 0), (1, 1)$
  - $(1, 0), (2, 0), (2, 1)$
  - $(0, 0), (1/2, 0), (1/2, 2)$
9. Find the volume of the region bounded by  $y = 1 - x^2$  and  $y = 0$ , rotated around...
  - $x = 1$
  - $y = 1$
10. Prove that  $e^x$  and  $e^{-x}$  intersect exactly once.
11. Find the volume of a pyramid with height 1 and a square base of side length 1.