I started mentoring students and postdocs thirty years ago, as a young assistant professor at Cornell. This continued after I moved to Berkeley in 1995, and I now enjoy working with young scholars in Germany. I always thought of mentoring as one of the best parts of my job.

With these notes, I’d like to share some anecdotes and experiences. These might be useful for colleagues who are starting their first tenure-track job, and is perhaps entertaining and thought-provoking for all readers. Before beginning, I would like to use this opportunity to thank all my students and postdocs. I learned a lot from you. Please continue to teach me.

**Doing the Opposite.** My first PhD student was slightly older than me. He came to my office once a week, for an entire afternoon, asking me for advice on his research. I eagerly offered my advice. After having left he did precisely the opposite of what I had suggested. The same happened in the following week. I recommended A, he did not-A. The same events, week after week. I was puzzled. Is that what it meant to be an advisor? The answer is yes, for this particular student. Having already made up his mind on what to do, he just needed me to test his ideas. And to argue. He became a respected professor at a top institution.

**A Threat.** It did not go so well with another student. One day, he messed up badly in presenting some material in a graduate seminar. I told him what I thought, right then and there. He was extremely upset because he felt humiliated in front of his peers. He threatened to shoot me if I ever did this again. I learned my lesson and decided to be more respectful.

**Finding Good Students.** Don’t ever compare students at your current institution with yourself or your peers, back when you were a grad student. Most students are capable and motivated. Don’t worry whether they are “good” yet. It is you who will make them good.

**Being an Imposter.** When I was a postdoc, I could not believe my luck. Someone paid me for what I loved doing. But how come they missed that I was not qualified for the job? That worried me. I was sitting in seminars and did not understand. I went to the library and the math books were incomprehensible. But everyone else seemed on top of it. I decided to wait and see. Surely, some day they’ll discover that I am a fraud. But this has not happened yet.

**Fordern und Fördern.** This is a phrase in German which my father liked to say. It is composed of two verbs, and translates roughly into “demand and encourage.” I have been awfully demanding towards my mentees, but I also strongly encourage them. Try to read that German phrase aloud. Pay attention to the umlaut. It sounds pretty nice, doesn’t it?
Follow the Child. When my children entered preschool, I learned about Maria Montessori’s famous line “Follow the Child.” She was absolutely right. You have to trust your children. They will show you what they need. You should likewise trust your students and postdocs.

Questions. Here are questions I ask mentees when we first meet. What do you excel at? Do you enjoy teaching? What have you written lately? What is the difference between pure and applied mathematics? Do you like to compute? Where will you be ten years from now?

The Path Forward. Inexperienced professors like to say “I’ll just give it to student” when referring to loose ends from their past research publications. This almost never works. You’d better solve your own problems. Your students are either unable to do it, or they will choose their own problems. Instead, show your students a path forward. Their own path, not yours.

Excellence through Diversity. Some people believe that there is a conflict between fostering diversity and striving for academic excellence. I found the opposite to be true. True excellence is inclusive. If you wish to train students and postdocs for academic careers at top research schools, then my advice is to build a diverse, inclusive and supportive team.

Gender. Another lesson I learned from Montessori preschool: “everyone has their gifts and challenges.” This applies to all learners, including you and me. Sometimes people ask how I became so successful in training outstanding female mathematicians. I already revealed two of the secret ingredients: Respect and encouragement. These two go a long way. Try to learn who your mentees really are. Gender, gender identity, and sexual orientation matter.

Phase Transition. The research seminar or group meeting can be a tough place for young scholars. Tone and atmosphere are tremendously important. I found that active participation by women and members of other underrepresented groups makes a huge difference. There is a threshold in their participation rate, around 30% in my empirical experience, at which a phase transition occurs. Above that threshold, seminars are fun and productive for everyone.

On Writing Well. I often recommend William Zinsser’s classic book with that title. But there are also good texts on mathematical writing. Writing a dissertation is writing. Writing research papers is writing. Writing job applications is writing. Writing grant proposals is writing. The importance of writing skills cannot be overemphasized. The mentor makes a huge difference. Lead by example. And, make them read aloud the writings they produce.

On Lecturing Well. Almost all mathematicians end up in careers where they must give clear and persuasive presentations. This is obvious for teachers and professors, but it also applies to those working in industry or government. Nobody is born a good lecturer. Practice makes all the difference. I discovered that some of the best-prepared incoming PhD students were on the debate team, back in their high school. Everyone else must catch up with those.

On Coding Well. To me, our cell phones are supercomputers. All of us spend most of the day performing heavy computations with these machines. But many young mathematicians are still afraid of using mathematical software for their research. Help your mentees to overcome that reluctance, and to make friends with tools like Julia, Macaulay2, Magma, Maple, Mathematica, Matlab, OSCAR, R, SAGE, etc. Do admire the output of their computations.
Listening. Prospective graduate students recently visited Berkeley. Before the visit day, my current students were asking me “What should we tell them?” I reply “Nothing, just listen to them.” At all stages of mentoring, listening is often more beneficial than telling things.

Being a Scholar. There are many ways to becoming a scholar. Here are two points I recommend to my mentees. First, learn about mathematics. Here is a good exercise: for each of the two-digit numbers xx in the Mathematics Subject Classification, from “03 Logic” to “94 Information and Communications,” state in your own words what xx is about. Name one person you know who works in xx. Second, find out about the history of your speciality. Read papers that were written more than 100 years ago. Don’t fear foreign language sources.

Matchmaking. After we got married in 1990, my wife and I traveled Korea by car. On a country road we picked up a hitchhiker, an old lady who was a professional matchmaker. When she learned that my wife and I had not used a matchmaker, she was shocked: how was it possible for us to meet in Seattle, without the services of her profession? That old lady had a good point. Matchmakers are useful. That is why I am a matchmaker for doing mathematics. I connect my mentees to others scholars. Many good matches came from this.

Holomorphic Vector Bundles. I believe the phrase “Good things happen to those who show up.” Encounters can be planned or circumstance. But if you don’t show up then you will miss out. Students are hesitant to attend colloquia because they don’t understand anything. (Like all imposters). But think of a language immersion class overseas. Just keep going. A few months later you will understand and speak. One colleague recommended uttering foreign words over and over again. You will learn their meaning by gauging the reaction of the listeners. Like a toddler. He said he tested this when he was a PhD student. He wanted to know what “holomorphic vector bundle” means. So, he went around and repeated those words over and over again. Now he is a senior researcher in complex geometry.

Waking up to E-Mail. Every mentor has a different style. So does every mentee. A while back, PhD students at Berkeley complained that they do not get enough attention from their advisors. My students think that they receive too much attention from their advisor. A friend once referred to my style as “the samurai method.” Receiving a barrage of e-mails, usually sent between 4am and 5am, is fine for some but not for others. Luckily, there is a very good mentor for everyone. Let’s all help young scholars in finding that perfect match.

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