Math 127, **Homework # 2** due: Thursday, February 15

- (1) Write a short essay ( $\leq$  one page) about the **genetic code**. Define the terms **codon** and **codon bias**. What is a **stop codon** ?
- (2) The HMM for the occasionally dishonest casino is specified by 1296 homogeneous polynomials  $p_{\tau_1\tau_2\tau_3\tau_4}$  in twelve unknowns  $\theta_{\bullet\bullet}, \theta'_{\bullet\bullet}$ . For which sequence of dice roll observations  $\tau_1\tau_2\tau_3\tau_4$  is the number of terms in the monomial expansion of  $p_{\tau_1\tau_2\tau_3\tau_4}$  maximal resp. minimal.
- (3) Compute (e.g. using MATLAB or Mathematica) the dimension of the vector space (over the field of real numbers) spanned by the 1296 coordinate polynomials  $p_{\tau_1\tau_2\tau_3\tau_4}$  of the occasionally dishonest casino model.
- (4) Prove Proposition 2.4 on page 46 in the ASCB book.
- (5) Let G be the undirected graph on five nodes with adjacency matrix

$$D_G = \begin{pmatrix} 0 & 3 & 7 & \infty & 11 \\ 3 & 0 & 8 & 4 & 2 \\ 7 & 8 & 0 & 1 & 5 \\ \infty & 4 & 1 & 0 & 20 \\ 11 & 2 & 5 & 20 & 0 \end{pmatrix}$$

Compute the tropical matrix powers  $D_G^2$ ,  $D_G^3$ ,  $D_G^4$ ,  $D_G^5$  and  $D_G^6$ . Also compute the tropical determinant of the 5 × 5-matrix  $D_G$ . Explain what the results of your computations mean.

- (6) Explain (in your own words) the proof of Remark 2.31 on page 68 in the ASCB book. Give several examples which illustrate this statement.
- (7) On Monday, February 12 at 8:00pm, Arnold Levine of IAS Princton will give a public lecture at the Berkeley Repertory Theatre on "The Evolution of Influenza Viruses in the 20th and 21st Centuries", and on Tuesday, February 13 at 3:00pm, he'll speak at MSRI on "DNA/RNA Sequence Complexity: The Entropy Distribution of Viruses and Bacteria". See www.msri.org for details. Attend (at least) one of these two lectures and write a brief report (≤ one page) on its content, highlighting what you see as the main insights presented by the speaker.