## DO NOT TURN OVER UNTIL INSTRUCTED TO DO SO.

## NO CALCULATORS PERMITTED.

## EXAM TIME IS 60 MINUTES.

## THE EXAM CONSISTS OF 5 QUESTIONS.

Your name: $\qquad$
Your SID: $\qquad$
Your Section and GSI: $\qquad$

| Question 1 | $/ 20$ |
| :--- | :--- |
| Question 2 | $/ 20$ |
| Question 3 | $/ 20$ |
| Question 4 | $/ 20$ |
| Question 5 | $/ 20$ |
| Total | $/ 100$ |

1. (a) Prove

$$
\log _{b}(s t)=\log _{b}(s)+\log _{b}(t)
$$

(b) Solve

$$
\ln (x)+\ln (x-1)=1
$$

2. Sketch the graph of the following rational function

$$
f(x)=\frac{x^{2}-1}{x^{4}-16}
$$

3. Evaluate the following expressions
(a) $\log _{81}(27)$
(b) $81^{-\frac{3}{4}}$
(c) $e^{2 \ln (3)+\ln (5)}$
(d) $\operatorname{area}\left(\frac{1}{x}, 1, e^{\frac{1}{2}}\right)$
4. (a) Write down an equation for a circle around $(1,2)$ with radius 3
(b) Write down an equation for the ellipse obtained from (a) by stretching the coordinate system by a factor of 2 horizontally and a factor of 3 vertically
(c) What are the area and coordinates of the center of the ellipse from (b)
5. You deposit $\$ 50$ in a bank account which promises an annual interest rate of $5 \%$.
(a) Write an expression for the amount of money in the account after $t$ years have passed, assuming that the bank compounds interest monthly.
(b) Write an expression for the amount of money in the account after t years have passed, assuming that the bank compounds interest continuously.
(c) If interest is compounded continuously, how long will it take before you have $\$ 200$ ?

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