## DO NOT TURN OVER UNTIL INSTRUCTED TO DO SO.

## NO CALCULATORS PERMITTED.

## EXAM TIME IS 50 MINUTES.

## THE EXAM CONSISTS OF 5 QUESTIONS.

Your name: $\qquad$
Your SID: $\qquad$

| Question 1 | $/ 20$ |
| :--- | :--- |
| Question 2 | $/ 20$ |
| Question 3 | $/ 20$ |
| Question 4 | $/ 20$ |
| Question 5 | $/ 20$ |
| Total | $/ 100$ |

1. Solve the following inequality. Express your answer as an interval.

$$
\frac{x-1}{x+1}>0
$$

2. Give an example of two functions $f, g: X \rightarrow X$, where $X$ is a set you may choose, such that

$$
\begin{equation*}
f \circ g \neq g \circ f \tag{1}
\end{equation*}
$$

3. (a) If a line $L$ has slope $m \neq 0$, what is the slope of a line $L^{\prime}$
i. perpendicular to $L$
ii. parallel to $L$
(b) Sketch the line $L: y=2 x+1$ and point $P:(2,0)$
(c) Write down the equation for the line $L^{\prime}$ perpendicular to $L$ passing through $P$
(d) Find the coordinates of the point of intersection of $L$ with $L^{\prime}$
4. Let $f(x)=|x+1|-|x-1|$
(a) Plot the graph of $f(x)$
(b) Is $f(x)$ a one-to-one function? Justify your answer.
(c) Is $f(x)$ an even or odd function? Justify your answer.
(d) Plot the graph of $\frac{1}{2} f(x+2)+2$ using simple transformations of $f(x)$
5. (a) Complete the square of $x^{2}+2(a-1) x+a^{2}$ and find the coordinates of the vertex of the parabola, when $x^{2}+2(a-1) x+a^{2}$ is viewed as a function in $x$
(b) By (a) or another method find all real numbers $a$ such that the quadratic equation $x^{2}+2(a-1) x+a^{2}=0$ in $x$ has
i. No solution in $x$
ii. One solution in $x$
iii. Two solutions in $x$

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