## MATH 1A MIDTERM 1 (001) PROFESSOR PAULIN



Name:

Student ID: \_\_\_\_\_

GSI's name: \_\_\_\_\_

Midterm 1 (001)

This exam consists of 5 questions. Answer the questions in the spaces provided.

- 1. Determine the domains of the following functions:
  - (a) (15 points)

$$\ln(\frac{1-x}{x-2})$$

Solution:



=) Domain of 
$$l_n\left(\frac{l-x}{n-z}\right)$$
 is  $\left(\frac{l-z}{n-z}\right)$ 

(b) (10 points)

$$\frac{1}{\sqrt{\arccos(x)}}$$

Solution:  

$$y = \operatorname{arccos}(x)$$
  $\operatorname{arccos}(x) > 0 \iff x$  in  $(-1, 1)$   
 $-1$   $x = 0$  Domain  $x \neq \frac{1}{\sqrt{\operatorname{arcos}(x)}}$  is  $(-1, 1)$ 

2. (a) (15 points) Describe in words, how, starting with the graph y = 2 + 3f(1-x), one can draw the graph

$$y = 1 - 3f(2x + 1).$$

Solution:

(b) (10 points) Simplify the following:

 $\arccos(\cos(4))$ 



Solution:

PLEASE TURN OVER

3. Calculate (using the limit laws) the following limits. If a limit does not exist determine if it is  $\infty$ ,  $-\infty$  or neither.



4. (25 points) Let  $f(x) = \begin{cases} 1 & \text{if } x \le 1 \\ 3 - 2x & \text{if } x > 1 \end{cases}$ .

Prove, using  $\epsilon, \delta$  methods, that f is continuous at x = 1. Solution:



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5. (25 points) Does there exist a tangent line to the curve

$$y = \frac{x+2}{x+1}$$

which contains the point (-1,1)? Carefully justify your answer. If you calculate a derivative do so using the limit definition. You do not need to use  $\epsilon, \delta$  methods. Solution:

 $f(x) = \frac{x+c}{c}$  $f'(a) = \lim_{h \to a} \frac{F(a+h) - F(a)}{h} = \lim_{h \to a} \frac{a+h+1}{h}$ h (a+h+z)(a+1) - @+z)(a+h+1)  $\geq$ 4-30 h(a+h+1)(a+1)2 4-20 h(a+h+1)(a+1) $\begin{array}{ccc} lim & -1 \\ h \to 0 & (a+h+1)(a+1) \end{array} = \frac{-1}{(a+1)^2} \end{array}$ Equation of tangent at  $x = a: y - \frac{a+2}{a+1} = \frac{-1}{(a+1)^2} (x-a)$ (-1, 1) su tanget =)  $(-\frac{a+2}{a+1} = \frac{-1}{(a+1)^2}(-1-a)$  $1 - \frac{a+2}{a+1} = \frac{1}{a+1} = 3 + 1 - (a+2) = 1 = 3 - 1 = 1$ Hence no tangent contains (-1,1).

END OF EXAM