This talk will review some of the connections established in recent years between the theory of excursions of Brownian motion and related stochastic processes and the asymptotics of various combinatorial objects such as random mappings, trees, forests, and partitions.