

You must always justify your answers. This means: show your work, show it neatly, and when in doubt, use words (and pictures!) to explain your reasoning. No justification = no points.

1. (5 pts) Evaluate the integral  $\int_0^4 y e^{-y/2} dy$ .

We integrate by parts, taking  $u = y$  and  $dv = e^{-y/2} dy$ , whence  $v = \frac{e^{-y/2}}{-1/2} = -2e^{y/2}$ :

$$\begin{aligned}\int_0^4 y e^{-y/2} dy &= \left[ y(-2)e^{-y/2} \right]_0^4 - \int_0^4 (-2)e^{-y/2} dy \\ &= 4(-2)e^{-4/2} - 0(-2)e^0 + 2 \int_0^4 e^{-y/2} dy \\ &= -8e^{-2} + 2 \left[ (-2)e^{-y/2} \right]_0^4 \\ &= -8e^{-2} - 4e^{-2} + 4e^0 \\ &= \boxed{4 - 12e^{-2}}\end{aligned}$$

2. (5 pts) Evaluate the integral  $\int \tan^3 \theta \sec^5 \theta d\theta$ .

We recognize  $\tan \theta \sec \theta d\theta = d(\sec \theta)$ , and  $\tan^2 \theta = \sec^2 \theta - 1$ . Thus, we substitute  $u = \sec \theta$ :

$$\begin{aligned}\int \tan^3 \theta \sec^5 \theta d\theta &= \int (\sec^2 \theta - 1) \sec^4 \theta \tan \theta \sec \theta d\theta \\ &= \int (u^2 - 1) u^4 du \\ &= \int (u^6 - u^4) du \\ &= \frac{u^7}{7} - \frac{u^5}{5} + C \\ &= \boxed{\frac{\sec^7 \theta}{7} - \frac{\sec^5 \theta}{5} + C}\end{aligned}$$

3. (0 pts) Can you make my currently scheduled office hours? Would you rather have Monday and/or Wednesday office hours from 4 to 4:45? Consider that moving Monday's office hours later means no office hours before the quiz on Monday.