

Moving Zeroes

What happens to the zeros of $z^2 - t$ as you move t along the real axis in the complex plane? What happens to the zeros of $f(z) - t$ when f is an arbitrary polynomial? What happens to the zeros of $f(z, t)$ when f is an arbitrary polynomial in two variables? Try to work with a few examples and then generalize.