## Math 1A Midterm 1 2005-9-29 11:00-12:30pm.

You are allowed 1 sheet of notes. Calculators are not allowed. Each question is worth 3 marks, which will only be given for a clear and correct answer.

1. Find the domain of the function $g(u)=\sqrt{u}+\sqrt{2-u}$.
2. Sketch the graph of $y=\left|x^{2}-2 x\right|$.
3. Find a formula for the inverse of the function $f(x)=1+e^{x^{3}}$.
4. Sketch the graph of a function $f$ that satisfies the conditions

$$
\lim _{x \rightarrow 0^{-}} f(x)=1, \lim _{x \rightarrow 0^{+}} f(x)=-1, \lim _{x \rightarrow 1^{-}} f(x)=1, \lim _{x \rightarrow 1^{+}} f(x)=-1, f(2)=1 .
$$

5. Evaluate the limit

$$
\lim _{x \rightarrow 1} \frac{x^{3}-1}{x^{2}-1}
$$

6. How close to 2 do we have to take $x$ so that $5 x+3$ is within a distance of 0.01 from $13 ?$
7. Find the numbers at which $f$ is discontinuous, where $f$ is defined by $f(x)=x^{2}$ if $x \leq 1, f(x)=1 / x$ if $1<x<3, f(x)=1 / 2+\sqrt{x-3}$ if $x \geq 3$.
8. What is

$$
\lim _{x \rightarrow-\infty} \frac{(3 x+1)(4 x+1)}{(x+1)(2 x+1)}
$$

9. A curve has equation $y=f(x)$. Write an expression for the slope of the secant line through the points $(3, f(3))$ and $(x, f(x))$, and write an expression for the slope of the tangent line at $(3, f(3))$.
10. If $g(x)=x^{3}+x^{2}+x+1$, find $g^{\prime}(0)$ and use it to find an equation of the tangent line to the curve $y=x^{3}+x^{2}+x+1$ at the point $(0,1)$.
11. Sketch the graph of the function $y=x^{2}|x|$, say where it is differentiable, and find a formula for its derivative.
12. Differentiate the function $y=e^{x+1}+4 \pi^{2}+(x+1) / \sqrt{x}$
13. At what point on the curve $y=1+2 e^{x}-3 x$ is the tangent line parallel to the line $3 x-y=5$ ?
14. Differentiate $x e^{x}(\sqrt{x}+1)$
15. Differentiate

$$
\frac{x^{2}}{1+1 / x}
$$

