

§6.4#42

Let  $X$  be a r.v. whose value is the number of balls that end up in the first bin. Then

$$X = X_1 + X_2 + \cdots + X_m$$

where each  $X_i = \begin{cases} 1 & \text{if ball } i \text{ ends up in bin 1} \\ 0 & \text{o/w} \end{cases}$

Note that  $E[X_i] = 1 \cdot P(X_i = 1) + 0 \cdot P(X_i = 0) = \frac{1}{n}$ . So by linearity of expectations

$$E[X] = E[X_1] + \cdots + E[X_m] = \frac{m}{n}$$

§8.1#6

For this problem, R=Reflexive, S=Symmetric, T=Transitive, A=Antisymmetric. To get full credit, you would need to justify your answers.

- (a) S
- (b) R, S, T
- (c) R, S, T
- (d) A
- (e) R, S
- (f) S
- (g) T, A
- (h) S