1. Let f be the function from $[0, 1]$ to the reals which is zero on the irrationals and takes a rational number in lowest form p/q to $1/q$. Does $\int_0^1 f\, dx$ exist? If so, what is it?