Final Exam

Name _____

Student ID Number

Discussion Section Instructor

(If you don't remember your section instructor's name, give section time instead.)

Instructions:

- Wait until you are told to begin before looking at the questions.
- After being told to start, put your name on each page, in case they get separated.
- Write answers in the space provided, and turn in only the exam paper. Show enough work so that we can see how you got your answers.
- You may use one prepared sheet of notes. No other notes, books or calculators are allowed.
- There are 15 questions, on both sides of the page. All questions have equal value.

For grading use only			
1		9	
2		10	
3		11	
4		12	
5		13	
6		14	
7		15	
8		Total	

1. Evaluate the limit if it exists (possibly as an infinite limit).

(a)
$$\lim_{x \to 1} \frac{1}{\ln x}$$
 (b) $\lim_{x \to 1} \frac{1}{(\ln x)^2}$

2. Differentiate the function $y = \sin(\sin(\sin x))$.

3. Find (a) all local maxima and minima of the function

$$f(x) = \frac{x}{x^2 + 1},$$

and (b) the intervals of increase or decrease of f(x).

4. Find the linear approximation to the function $f(x) = \ln x$ near x = 2.

5. If $y = e^{xy}$, express dy/dx in terms of x and y.

6. Suppose we use Newton's method to approximate the root r of the function whose graph is shown, using $x_1 = 1$ for the first approximation.



For the next approximation x_2 , decide whether $x_2 < r$ or $x_2 > r$. Justify your answer.

7. Find the largest area of a rectangle with horizontal and vertical sides, lower-left corner at the origin (0,0), and upper-right corner on the curve $y = e^{-x}$.

8. Find the limit.

 $\lim_{x \to \infty} x^{1/(1 + \ln x)}$

9. If $\int_a^x f(t) dt = x \ln x$ for all x > 0, find the function f(x) and the constant a.

10. Evaluate the integral.

$$\int_0^2 x e^{-x^2} dx$$

11. Evaluate the indefinite integral.

$$\int \frac{(x+1)(x+2)}{x^2} \, dx$$

12. Sketch the region enclosed by the lines x = 2, y = 2 and the curve xy = 1, and find its area.

13. Find the average value of the function f(x) = 1/x on the interval [1, 3].

14. Find the volume of the circular cone obtained by rotating the triangle enclosed by the x and y axes and the line x + y = 1 about the y axis. (Solve the problem using integration. Do not just cite a formula you might already know for the volume of a cone.)

15. Set up, but do not evaluate, an integral for the volume of the solid obtained by rotating the region enclosed by the x axis, the line x = 2, and the curve $y = xe^{-x}$ about the y axis.