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Math128B: Numerical Analysis

Homework #6, Due March 8, 2010

- **Section 8.6:** Problems 2, 4, 8, 9, 10.
- The Toeplitz matrix is a matrix whose entries remain constant along each diagonal. For example, the following is a 4×4 Toeplitz matrix

$$T_4 = \begin{pmatrix} a_0 & a_1 & a_2 & a_3 \\ a_{-1} & a_0 & a_1 & a_2 \\ a_{-2} & a_{-1} & a_0 & a_1 \\ a_{-3} & a_{-2} & a_{-1} & a_0 \end{pmatrix}.$$

Let T be an $n \times n$ Toeplitz matrix and let x be an n -dimensional vector. Show how to compute the matrix-vector product Tx in $O(n \log n)$ operations using the FFT.

- **Section 9.1:** Problems 2b, 4, 6b, 7, 8, 9, 10, 12, 14.