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## Math128B: Numerical Analysis

### Homework #5, Due March 2, 2009

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- **Section 8.6:** Problems 2, 4, 8, 9, 10.
- The Toeplitz matrix is a matrix whose entries remain constant along each diagonal. For example, the following is a  $4 \times 4$  Toeplitz matrix

$$T_4 = \begin{pmatrix} a_0 & a_1 & a_2 & a_3 \\ a_{-1} & a_0 & a_1 & a_2 \\ a_{-2} & a_{-1} & a_0 & a_1 \\ a_{-3} & a_{-2} & a_{-1} & a_0 \end{pmatrix}.$$

Let  $T$  be an  $n \times n$  Toeplitz matrix and let  $x$  be an  $n$ -dimensional vector. Show how to compute the matrix-vector product  $Tx$  in  $O(n \log n)$  operations using the FFT.