

# MANY CHEERFUL FACTS

presents

## “Nine Magic Discriminants”

a talk by Matthew Satriano

13:10 – 14:00 on Thursday, November 15, in room 1015.

Many of us are probably familiar with the result that the ring of integers of the imaginary quadratic field  $\mathbb{Q}(\sqrt{-d})$  is a PID if and only if  $d = 1, 2, 3, 7, 11, 19, 43, 67,$  or  $163$ . But probably not too many of us have ever seen a proof. After saying a few words about the very interesting history of this class number problem, I'll present Heegner's proof, which relates the question to modular forms and a certain degree 24 polynomial.

*I am the very model of a modern Major General,  
I've information vegetable, animal, and mineral,  
I know the kings of England, and I quote the fights historical  
From Marathon to Waterloo, in order categorical;  
I'm very well acquainted, too, with matters mathematical,  
I understand equations, both the simple and quadratical,  
About binomial theorem I'm teeming with a lot o' news,  
With many cheerful facts about the square of the hypotenuse!*

— Gilbert & Sullivan,  $P \circ P$

The website for Many Cheerful Facts is  
<http://www.math.berkeley.edu/~mcf>