

Name:

1. Let  $A$  be an  $n \times n$  matrix with eigenvalue  $\lambda$ . For each of the following statements, write the word “true” or “false.”

(a) The matrix  $2A$  has eigenvalue  $2\lambda$ .

(b) The matrix  $A + 2I$  has eigenvalue  $\lambda + 2$ .

2. Give an orthogonal matrix  $Q$  and a diagonal matrix  $\Lambda$  such that  $A = Q\Lambda Q^{-1}$ .

$$A = \begin{pmatrix} 4 & 1 & 1 \\ 1 & 4 & 1 \\ 1 & 1 & 4 \end{pmatrix}$$