

Name:

1. For each of the following statements, write the word “true” or “false.”

(a) Let  $f(x)$  be an odd function and  $g(x)$  be an even function. Then  $f(x)g(x)$  is an odd function.

(b) Let  $f(x)$  be an odd function and  $g(x)$  be an even function. Then  $f(x) + g(x)$  is an odd function.

2. Find the Fourier series for the function  $f(x)$  defined by

$$f(x) = \begin{cases} -x^2 + \pi^2 & \text{if } -\pi \leq x \leq 0 \\ x^2 - \pi^2 & \text{if } 0 < x < \pi \end{cases}$$

and  $f(x + 2\pi) = f(x)$  for any  $x$ .