

**MATH 74 HOMEWORK 3**  
**DUE MONDAY, SEPTEMBER 15TH**

- (1) Do Eccles, 4.1, 4.2, 6.5.
- (2) Let  $C$  be a set and let  $A$  and  $B$  be subsets of  $C$ . Prove *De Morgan's Laws*:
  - (a)  $C \setminus (A \cup B) = (C \setminus A) \cap (C \setminus B)$ , and
  - (b)  $C \setminus (A \cap B) = (C \setminus A) \cup (C \setminus B)$ .
- (3) Write out the power sets of the sets  $\emptyset$ ,  $\{1\}$ ,  $\{1, 2\}$ , and  $\{1, 2, 3\}$ . Make a conjecture of the form “If  $A$  is a finite set with  $n$  elements, then the power set of  $A$  is a set with \_\_\_ elements.” (Bonus: prove your conjecture.)
- (4) Let  $X = \{1, 2\}$  and let  $Y = \{2, 3\}$ . Compute the power set of  $X \times Y$ , the Cartesian product of  $X$  and  $Y$ .
- (5) Let  $X = \{1, 2, 3\}$  and  $Y = \{1, 2, 3, 4\}$ . Count the number of functions from  $X$  to  $Y$ , preferably without actually writing them all down. (If I haven't defined “function” by the end of Friday's lecture, then don't do this problem).