

# Math 1A

## Quiz 5 - October 7, 2009

Name: KEY

1. Find  $y'$  if  $x^2 + xy^2 = \sin y$

Use implicit differentiation:  $2x \left(\frac{dx}{dx}\right) + (1 \cdot \frac{dx}{dx}) \cdot y^2 + (x) \cdot (2y \frac{dy}{dx}) = \cos y \frac{dy}{dx}$

Solve for  $y'$ :  $2x + y^2 + 2xy \cdot y' = y' \cdot \cos y$

$$2x + y^2 = y' \cos y - 2xy \cdot y'$$

$$2x + y^2 = y' (\cos y - 2xy)$$

$$y' = \frac{2x + y^2}{\cos y - 2xy}$$

2. Use log rules to simplify as best you can,  $\ln(\cos^4(x) \cdot \sin(x) \cdot e^x)$

$$= \ln(\cos^4 x) + \ln(\sin x) + \ln(e^x)$$

$$= 4 \ln(\cos x) + \ln(\sin x) + x$$

(Something to think about: If I had asked you to find the derivative of this function, would you have simplified it first this way, or used a messy combination of product and chain rules. Be alert for problems like this!)

3. Find the derivative of the following functions:

(a)  $(17)^x$

$$17^x \cdot \ln 17$$

(b)  $y = e^x \cdot x^{\sin x}$

$$\ln y = \ln(e^x \cdot x^{\sin x}) = \ln e^x + \ln(x^{\sin x})$$

$$\ln y = x + \sin x \ln x$$

Take derivatives:

$$\frac{1}{y} \cdot \frac{dy}{dx} = 1 + \cos x \cdot \ln x + \frac{\sin x}{x}$$

$$\frac{dy}{dx} = y \left( 1 + \cos x \ln x + \frac{\sin x}{x} \right) = e^x x^{\sin x} \left( 1 + \cos x \ln x + \frac{\sin x}{x} \right)$$