

Math 1A

Quiz 3 - September 16, 2009

Name: Key

1. Evaluate the following limits. If no limit exists, briefly say why.

$$(a) \lim_{x \rightarrow 2} \frac{x^2 + x - 6}{x^2 - 4} = \lim_{x \rightarrow 2} \frac{(x+3)(x-2)}{(x+2)(x-2)} = \lim_{x \rightarrow 2} \frac{x+3}{x+2} = \boxed{\frac{5}{4}}$$

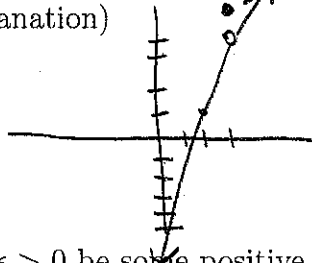
$$(b) \lim_{x \rightarrow 0} \frac{\sqrt{3+x} - \sqrt{3}}{x} \cdot \frac{(\sqrt{3+x} + \sqrt{3})}{(\sqrt{3+x} + \sqrt{3})} = \lim_{x \rightarrow 0} \frac{(3+x) - (3)}{x(\sqrt{3+x} + \sqrt{3})} = \frac{x}{x(\sqrt{3+x} + \sqrt{3})}$$

$$= \lim_{x \rightarrow 0} \frac{1}{\sqrt{3+x} + \sqrt{3}} = \frac{1}{\sqrt{3} + \sqrt{3}} = \boxed{\frac{1}{2\sqrt{3}}}$$

2. Let

$$f(x) = \begin{cases} 3x - 5 & \text{if } x \neq 3 \\ 5 & \text{if } x = 3 \end{cases}$$

(a) Sketch a graph of $y = f(x)$. Where is $f(x)$ not continuous? (Give a BRIEF explanation)



f is not continuous when $x=3$

because $\lim_{x \rightarrow 3} f(x) \neq f(3)$

(b) Let $\epsilon > 0$ be some positive number. Find a $\delta > 0$ so that if $0 < |x - 3| < \delta$ then $|f(x) - 4| < \epsilon$.

$$|f(x) - 4| < \epsilon$$

$$|(3x - 5) - 4| < \epsilon$$

$$|3x - 9| < \epsilon$$

$$3|x - 3| < \epsilon$$

$$|x - 3| < \epsilon/3$$

Choose $\delta = \epsilon/3$.

(c) Can you find a different value of δ which works?

Any smaller positive value of δ will work, e.g. $\epsilon/10$.